

Additional Problems

Evaluate Limits

Differential Calculus**201-MA1-DW**

Exercises: Find the following limits, if exist.

1. $\lim_{x \rightarrow 3} \frac{x^2 - x - 6}{x^2 + x - 12}$

2. $\lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x^2 + 5x - 14}$

3. $\lim_{x \rightarrow 1} \frac{2x^2 - x - 1}{x^2 + x - 2}$

4. $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x^2 + 4x - 21}$

5. $\lim_{x \rightarrow -1} \frac{x^2 + 2x + 1}{x^2 + 4x + 3}$

6. $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 + 2x - 8}$

7. $\lim_{x \rightarrow -2} \frac{x^2 - 4}{x^3 + 8}$

8. $\lim_{x \rightarrow 1} \frac{x^3 - x^2}{x^2 + 8x - 9}$

9. $\lim_{x \rightarrow 1} \frac{x^2 - x - 2}{x^2 - 6x - 7}$

10. $\lim_{x \rightarrow 2} \frac{3x^2 - 4x - 4}{x^2 - 4}$

11. $\lim_{x \rightarrow -2} \left\{ \frac{2x^3 - 8x}{x + 2} \right\}^2$

12. $\lim_{x \rightarrow 0} \frac{\frac{1}{2+x} - \frac{1}{2}}{x}$

13. $\lim_{x \rightarrow 0} \frac{\frac{1}{3+x} - \frac{1}{3}}{x}$

14. $\lim_{x \rightarrow 1} \frac{\frac{1}{1+x} - \frac{2}{x-1}}{x-1}$

15. $\lim_{x \rightarrow 2} \frac{\frac{x}{5+x} - \frac{2}{7}}{x-2}$

16. $\lim_{x \rightarrow -3} \frac{x^2 - 9}{\frac{x}{x+8} + \frac{3}{5}}$

17. $\lim_{x \rightarrow 3} \frac{20x - 60}{x^3 + 4x^2 - 21x}$

18. $\lim_{x \rightarrow -1} \frac{x+1}{x^3 + 3x^2 + 2x}$

Answers:

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|--------------------|---------------------|-------------------|------------------|--------------------|--------------------|-------------------|
| 1. $\frac{5}{7}$ | 2. $\frac{1}{3}$ | 3. 1 | 4. $\frac{3}{5}$ | 5. 0 | 6. 2 | 7. $-\frac{1}{3}$ |
| 8. $\frac{1}{10}$ | 9. $\frac{1}{6}$ | 10. 2 | 11. 256 | 12. $-\frac{1}{4}$ | 13. $-\frac{1}{9}$ | 14. $\frac{1}{4}$ |
| 15. $\frac{5}{49}$ | 16. $-\frac{75}{4}$ | 17. $\frac{2}{3}$ | 18. -1 | | | |

Exercises: Find the following limits, if exists.

19. $\lim_{x \rightarrow 1} \frac{x-1}{\sqrt{x+3} - 2}$

20. $\lim_{x \rightarrow 2} \frac{x-2}{\sqrt{2x+5} - 3}$

21. $\lim_{x \rightarrow 4} \frac{x-4}{\sqrt{3x+4} - 4}$

22. $\lim_{x \rightarrow 2} \frac{\sqrt{5x+6} - 4}{x-2}$

23. $\lim_{x \rightarrow 7} \frac{\sqrt{3x+4} - 5}{x-7}$

24. $\lim_{x \rightarrow 2} \frac{\sqrt{2x} - 2}{x-2}$

25. $\lim_{x \rightarrow 2} \frac{x-2}{3 - \sqrt{x^2+5}}$

26. $\lim_{x \rightarrow 2} \frac{x-2}{4 - \sqrt{3x^2+4}}$

27. $\lim_{x \rightarrow 2} \frac{\sqrt{2x^3+9} - 5}{x-2}$

Answers:

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|--------------------|--------------------|-------------------|-------------------|--------------------|-------------------|--------------------|
| 19. 4 | 20. 3 | 21. $\frac{8}{3}$ | 22. $\frac{5}{8}$ | 23. $\frac{3}{10}$ | 24. $\frac{1}{2}$ | 25. $-\frac{3}{2}$ |
| 26. $-\frac{2}{3}$ | 27. $\frac{12}{5}$ | | | | | |